

> Kingdom of Saudi Arabia
> King $\mathcal{A}$ bdulaziz University

Faculty of Science-Mathematics Department
First Mid-Term Exam (90 Minutes) - (204 Math). 23/8/1432 H - 24/7/2011 A.D. First Semester 1432-1433 H

Model A

| Name: | Section: |
| :--- | :--- |
| Student's I.N. : | Serial Number: |
|  |  |


| $Q_{1}$ | $Q_{2}$ | $Q_{3}$ | $Q_{4}$ | $Q_{5}$ | $Q_{6}$ | Total Marks (25) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |

## (Answer the following questions)

1 Choose the correct answer (writing details (iii) and (iv) only) [6 Marks]
(i) The order of differential equation $\frac{d^{2} y}{d x^{2}}+2\left(\frac{d y}{d x}\right)^{3}-y=e^{x}$ is third.
(a) true
(b) false
(ii) The differential equation $x d y=\left(x e^{x}-y-x y\right) d x$ is linear in $y$.
(a) true
(b) false
(iii) The differential equation $\frac{d y}{d x}=y(1-y)$ has the solution $y=1$ as
(a) a singular solution
(b) a particular solution
(iv) According to the Existence and Uniqueness Theorem the IVP:

$$
\frac{d y}{d x}=\sqrt{x y}, y(2)=1 \text { has }
$$

(a) unique solution
(b) an infinitely many solutions
(c) no solution

2 Solve the differential equation:

$$
\frac{d y}{d x}=\frac{x y+3 x-y-3}{x y-2 x+4 y-8}
$$

## 3 Solve the differential equation:

$$
x d x+\left(x^{2} y+4 y\right) d y=0, \quad y(4)=0
$$

4 Solve the differential equation:

$$
\frac{d y}{d x}=y\left(x y^{3}-1\right)
$$

## 5 Solve the differential equation:

$$
x \frac{d y}{d x}=y+\sqrt{x^{2}-y^{2}}
$$

## 6 Solve the differential equation:

$$
\frac{d y}{d x}=\frac{1-x-y}{x+y}
$$

